## EVALUATION TECHNIQUE IN THE SPI-CALCULUS FOR CRYPTOGRAPHIC PROTOCOLS

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# Abstract

Bisimulation as a technique could be well invested for proving authenticity and secrecy properties of cryptographic protocols to gain the legality of protocol optimization. In this paper, we will do some changes in the spi-calculus after the original work of M.Abadi and A.Gordon. Then we will introduce evade bisimulation following Abadi and Gordon's framed bisimulation proposal, in which a convenient proof technique is presented. It will impose minimality requirements on the environment and detect the limit beyond which the bisimilarity is kept valid and furthermore it will avoid quantification over contexts. Also, it will give a solution for input transitions for the case of finite processes. Based on the revised spi-calculus would be used to prove that evade bisimilarity, an equivalence relation, is decidable for main security properties: Authenticity and Secrecy.

Keywords: Cryptographic protocols, testing equivalence, Bisimulation, authenticity and secrecy

### 1. Introduction

The present era of modern developments is denoted by mobile communication. In this field a wide range of proposals have been adopted as a result of the increased utilization of internet applications for business transactions, E-commerce, exchanges of sensitive government information and enumerable military implementation tasks. A considerable development in telecommunication networks has contributed to the success of these applications. As all of these services take advantage of communication in distributed systems in which computers are no longer considered devices that operate in isolation. Conversely, they are now part of a global environment where local and remote resources can be shared.

The development of telecommunication networks has therefore encouraged the development of services that take advantage from the communication among different distributed environments. It is clear that most of these applications would not be applied without verifying the security decision.

The *spi-calculus* introduced by Abadi and Gordon [1] as an extension of the  $\pi$ -calculus [20, 19] with cryptographic primitives has been used for cryptographic protocols modeling. By the implementation of these tools, cryptographic protocols design is drawn for possible study and investigations to prove the main security properties of the authentication and secrecy. The major attempts focused on in this thesis are testing equivalence and bisimulation techniques in spi-calculus.

In general, through the bisimulation technique, two different systems could be decided as equivalent when a correspondence between their steps is established or not equivalent when no correspondence is approved. The correspondence involves system behavior steps and also the steps taken by its environment as reactions. In the bisimulation modeling, it is not necessary to model an environment explicitly neither to analyze its possible internal computations but all what is needed, is to forward the modeling aspect towards the overall interaction between the system from one side and the environment from the reaction side.

M.Abadi and A.Gordon defined the *Framed bisimilarity* method [2] as a trend to prove process equivalence based process-environment interactions. Their work represented a restricted attempt that necessitated the existence levels of quantification over infinite domains. Our work follows Abadi and Gordon's framed bisimulation proposal. It introduces *evade* bisimulation in which a convenient proof technique is presented. This technique is driven; it will detect the limit beyond which the bisimilarity is kept valid and avoid quantification over contexts. In this paper, we will also introduce a new variant of the spi-calculus suggested by [7]. Based on the revised spi-<sub>H</sub>-calculus would be used to prove that evade bisimilarity, an equivalence relation, is decidable for main security properties: *Authenticity and Secrecy*.

#### 2. THE Spi-<sub>H</sub>-CALCULUS

This section gives the syntax and informal semantics of the spi-<sub>H</sub>-calculus used by [7] with some changes, after the original work of Abadi and Gordon [1]. The assumptions of this work are built on shared-key cryptography.

# 2.1 Syntax

Names and operators construct the syntax of the spi- $_{\rm H}$ -calculus, primitively, and other structures are built on them. Protocol model, is a structure of representative spi- $_{\rm H}$ -calculus syntax. In this structure messages, expressions, logical formulae and processes define the attributes needed to express all the objects and the activities driven in establishing protocols. Table 1 summarizes the calculus.

Names  $\mathcal{N}$  range over communication channels, data (variables or clear texts and a message) or keys. Along the declaration, names are used alternatively through the syntax regardless of representations. Any name would be tagged to the type by its appearance order.

**Notation 1:** We reserve the lower case letters *a*, *b*, *ch* to denote channels and *k*, *l* to denote keys and *m*, *n* to denote messages.

Expressions are those descriptions that are obtained by applying encryption, decryption, paring and projection operators to names and ciphertext. For example, the expression  $\zeta$  is a cleartext, when it is encrypted using the value  $\eta$  as a key, the overall actions would be given by *Enc*  $\eta(\zeta)$ , yielding that  $\zeta$  as a

cleartext is encrypted under the key  $\eta$ , conversely the decryption action  $Dec_{\eta}\{\zeta\}$  stands to decrypt the ciphertext using the value of  $\eta$  as a key. We assume that a key should be a name and the encryption action uses shared key in modes simple and nested modes.

Logical formulae generalize the usual equality operator of the  $\pi$ -calculus by conjunction and negation. Moreover we introduce two new predicates  $[\zeta:\mathcal{N}]$  and  $[\zeta:\mathcal{M}]$ . The predicate  $[\zeta:\mathcal{N}]$  which tests for the format of the argument  $\zeta$ , whether it evaluates to a name or not, and the predicate  $[\zeta:\mathcal{M}]$  which test for the argument  $\zeta$ , whether it evaluates to a compound ciphertext or not, and with "*Let*" construct that binds the value of some expression  $\zeta$  to a name *z*.

A finite set of terms,  $T = \{t_1, t_2, ..., t_n\}$ . The difference from Abadi and Gordon [1] that in this one assume the set *T* to be defined, so that we can associate each state to a term *t*. In order to define the notion of *state* we have to introduce the definition of finite multisets.

**Definition 2:** A finite multiset  $\varpi$  over a set *L* is a map  $\varpi : L \to M$  such that  $\varpi^{-1}(M_1)$  is finite. We define the following operations on finite multisets:

a) The *difference* of the multisets  $\varpi$  and  $\varpi'$  is the multiset  $\varpi \mid \varpi'$  where  $(\varpi \mid \varpi')(l) = max(0, \varpi(l) - \varpi'(l));$ 

b) The *union* of two multisets  $\varpi$  and  $\varpi'$  is the multiset  $\varpi \bigcup \varpi'$  where  $(\varpi \bigcup \varpi')(l) = \varpi(l) + \varpi'(l)$ ;

c) We say that  $l \in \varpi$  iff  $\varpi$  (l) > 0.

We define formally our notion of *state* as follows:

**Definition 3:** We define a *state*,  $\sigma = \{\sigma_t\}_{t \in T}$ , to be a family of multisets indexed by the terms, where each

 $\sigma_t$  represents the local state of the term t. We denote the set of all states by  $\Sigma$ .

A first approach to the definition of state would be a family of sets. If we consider each  $\sigma_t$  as a set, we were restricting the possibility of a principal to have many copies of the same term. We want to deal with the possibility of existing several inputs of the terms and verify that our system has the desired properties for input transitions.

Processes are the different sequences of activities conducted along a protocol function. There are diverse forms of processes that have a distinct function for each. A process could be built using a set of operators that include standard  $\pi$ -calculus [20] and two new ones; Boolean guards and encryption/decryption. However, process forms are used to explain the following:

- 0, is a null process that dose nothing.
- An input process;  $\eta(x)$ . *P* represents input of a generic message *x* along  $\eta$ : the only useful case is when  $\eta$  is a name, otherwise the whole process is stuck.
- An output process  $\overline{\eta}\zeta P$  represents out of  $\zeta$  along the channel  $\eta$ . The only useful case is when  $\eta$  is a name and  $\zeta$  is a message, otherwise the whole process is stuck.
- Non-deterministic choice P + Q: can behave either as P or Q; the choice might either be triggereazed by the environment, or by internal computations of P or Q.
- Parallel composition  $P \mid Q$ ; is the parallel execution of P and Q.
- Restriction (va)P: creates a new name a which is only known to P.
- Replication *!P* behaves like many unbounded copies of *P* running in parallel, i.e.  $P | P | P | \dots$

• Boolean Guard  $\phi P$  behaves like P if the formula is logically true, otherwise is stuck.

• Encryption/Decryption let  $z = \zeta$  in P: attempts evaluation of  $\zeta$ : if the evaluation succeeds, the result bound to z within P, otherwise the whole process is stuck.

Usual calculus abbreviate (va)(vb) P into (va, b) P, and  $\overline{M}(N)$ . 0 into  $\overline{M}(N)$ . In the spi-<sub>H</sub>-calculus, processes are identified up to renaming of bound names. Bound names are the entities that are enclosed within a process definition P, and not those that have explicitly been tagged with any other outside the process. So the closed process will then be defined as the process that has no free variables; *Proc is used to define a set of closed processes*.

Let fn(P) denote the set of free names in P and fv(P) is the set of free variables in P, and alphaequivalence arises as expected, n(P) is  $fn(P) \cup bn(P)$ . In this context, similar notations are used for formulae, expressions and messages.

If two processes can be made equal by conflict-free renaming of bound names then they are alphaequivalent. Substitutions  $\sigma$  are mappings  $\{\zeta/x\}$  from names x to messages  $\zeta$ , following the usual assumption that name-capture is avoided through implicit alpha conversion. Substitutions are applied to processes, expressions and guards very simply as for example,  $P\{\zeta/x\}$  replace all free occurrence of x in P by  $\zeta$ , possibly renaming bound names in P avoiding name capture.

**Definition 4:** A substitution  $\sigma$  is a finite partial map from the set of names N to the set of messages M;  $\{M/x\}$ .

The definition shows the effect of applying a substitution  $\sigma$  to a process *P*. This is essentially to replace each free occurrence of each name (i.e.; *x*) in *P* by  $\sigma(x) = M$ , for some *x* and *M*. The mapping must, however, be done in such a way that unintended capture of names by binders is avoided Substitutions are applied to processes, expressions and guards in straightly, i.e.  $P\{M | x\}$  replace all free occurrence of x in *P* by *M*, possibly renaming bound names in *P* avoiding name capture.

Domain and its co-domain of  $\sigma$  are denoted as  $dom(\sigma)$  and  $range(\sigma)$  respectively .Let  $n(\sigma) = dom(\sigma) \cup \left(\bigcup_{M \in range(\sigma)} n(M)\right)$  When a tuple of distinct names  $\vec{x} = (x_1, x_2, ..., x_n)$  and a tuple of

messages  $\bar{M} = (M_1, M_2, ..., M_n)$  are given, the substitutions mapping of each  $x_i$  to  $M_i$  will be convenient. Usually a tuple is a set of its component.  $\sigma[\bar{M}/\bar{x}]$  is the substitution  $\sigma'$  which represents union of  $\sigma$  and  $[\bar{M}/\bar{x}]$ . Such case is referred to as  $\sigma'$  extends  $\sigma$ .

In the current syntax of spi-calculus, the assumptions on the cryptographic systems are recalled thus:

- 1– For perfect encryption the key k used for encrypting a message M in the form  $Enc_k(M)$  should be used for decrypting that message. Encrypting M under k can only produce the ciphertext. Thus, a hacker cannot decrypt the message M without knowing the encryption key k.
- 2- The assumptions necessitate that there is enough redundancy in the structure of messages to ensure whether the decryption of a message on a given key has actually succeeded or not and additionally, to verify the role (either a key or a compound ciphertext).
- 3– Strictly, a new key is created by using fresh names from a primitive set of names.

a,b,c,k,l,m,n,x,y,z		names N	
$\zeta,\eta ::= a$	$\frac{1}{  Enc_{\eta}(\zeta)   Dec_{\eta}(\zeta)}$	expression s 3	
	$\langle \zeta_1, \zeta_2 \rangle \mid \pi_1(\zeta) \mid \pi_2(\zeta)$	;)	
	$ \langle M_1, M_2 \rangle   Enc_k \{M\}$	messages M	
$\overline{\phi,\psi} ::= tt$	- $        -$	guards Φ	
Ì	$[\zeta = \eta]$	(equality)	
	$[\zeta:N]$	(is a name)	
	$\mid [\zeta:M]$	(is a decomposab ility)	
	let $z = \zeta$ in $\phi$	(decryption)	
P,Q,R::=		processes P	
	0	(null)	
	$\eta(x).P$	(input prefix)	
	$  \overline{\eta} \langle \zeta \rangle P$	(output prefix)	
	P Q	(parallel compositio n)	
	P+Q	(choice)	
	~ ! P	(replicatio n)	
	(vn)P	(restrictio n)	
	$\phi P$	(boolean guard)	
	let $z = \zeta$ in P	(encryption / decryption)	

# TABLE 1 Syntax of the Calculus

It is assumed that Dec.(.) does not occur in  $[\zeta : N]$ ,  $[\zeta = \eta]$ ,  $\eta(x)$ , and  $\overline{\eta}\langle \zeta \rangle$ . Operators a(x), (va), and let  $z = \zeta$  in . are binders, with the obvious scope, for names x, a and z, respective ly. In let  $z = \zeta$  in ., it is assumed that  $z \notin n(\zeta)$ 

# **2.2 Operational Semantics**

Two main evaluation modes are used in the operational semantics evaluation function. The first is utilized for expressions while the second is used for Boolean Guards. These two evaluations are denoted as follows:

- For an expression  $\overline{\cdot} : \varepsilon \to M \cup \{\bot\}$  where  $\bot$  is a distinct symbol  $(\bot \notin M)$ .
- For an evaluation of a Guard  $\cdot : \Phi \rightarrow \{tt, ff\}$ , is defined by induction on  $\Phi$ .

The evaluation function is defined recursively according to table 2. In this table, it is obvious that expression evaluations rely on the implementation of *let* and *guard* only. Hence, the decryption is bounded along this evaluation scheme.

As table 3 shows, the operational semantics of the spi-<sub>H</sub>-calculus used in our work. Let and guard items are used as primitive rules driven to decrypt messages. A process  $\Phi P$  behaves like P provided that  $\Phi$  evaluates to true, otherwise,  $\Phi P$  is stuck. A process let  $z = \zeta$  in P behaves like  $P\left\{\frac{\zeta}{\zeta}/z\right\}$  provided that the

evaluation of  $\zeta$  succeeds; otherwise, let  $z = \zeta$  in *P* behaves like  $P\left\{\frac{\zeta}{z}/z\right\}$  is stuck. Rule (E-OUT) details

the case when the environment receives a message M and updates its knowledge accordingly, and for the sake of a transition to occur, all channels are supposed to be well announced to the environment.

Rule (E-INP) details the case, when the environment sends a message M to the process. Message m is not arbitrary and the expression  $\zeta$  describes how this message is built out of the environment and of the names  $\overline{b}$  to define M. Creation of new names  $\overline{b}$  is recorded by  $[\overline{b}/\overline{x}]$ , and in this case a must belong to the knowledge of the environment to explain its announcement.

### 3. Evade Bisimulation

Based on the earlier works of framed bisimulation[7, 2], we concluded that their definition suffers from quantification over all possible contexts, and furthermore it does not overcome the general problem for the input transitions. Hence, the present work will solves these conducts to give a proper outcome overcoming universal quantification.

a	= <i>a</i>
$\overline{Enc_{\zeta}(\eta)}$	$=\begin{cases} Enc_k(M) & if \overline{\eta} = M \in \mathcal{M} \text{ and } \overline{\zeta} = k \in \mathcal{N} \\ \bot & otherwise \end{cases}$
$\overline{Dec_{\zeta}(\eta)}$	$= \begin{cases} M & \text{if } \overline{\eta} = Enc_k (M) \in \mathcal{M} \text{ and } \overline{\zeta} = k \in \mathcal{N} \\ \bot & \text{otherwise} \end{cases}$
$\overline{\left\langle \zeta_{1},\zeta_{2}\right\rangle }$	$= \begin{cases} \langle M_1, M_2 \rangle & if \ \overline{\zeta_1} = M_1 \text{ and } \overline{\zeta_2} = M_2, \\ for \text{ some } M_1 \text{ and } M_2 \\ \bot & otherwise \end{cases}$
for $i=1,2, \overline{\pi_i(\zeta)}$	$=\begin{cases} M_{i} & \text{if } \overline{\zeta} = \langle M_{1}, M_{2} \rangle, \text{ for some } M_{1} \text{ and } M_{2} \\ \bot & \text{otherwise} \end{cases}$
tt	= $tt$
$\overset{=}{\phi} \land \psi$	$= \phi \wedge \psi$
$\neg \psi$	$= \oint \wedge \psi$ $= \neg \psi$
let $z = \zeta$ in	$\phi = \begin{cases} \hline \phi \ \{M \ /x \ \} \\ ff & otherwise \end{cases} if  \zeta = M \in \mathcal{M}$
[ζ:Ν]	$= \begin{cases} tt & if \ \zeta \in \mathcal{N} \\ ff & otherwise \end{cases}$
[ζ:M]	$= \begin{cases} tt & if  \zeta \neq \perp \\ ff & otherwise \end{cases}$
$[\zeta = \eta]$	$= \begin{cases} tt & if  \zeta = \eta \in \mathcal{M} \\ ff & otherwise \end{cases}$

**TABLE 2** Evaluation in the spi -Calculus

TABLE .3 The Operational Semantics of the spi-Calculus

$$(OUT) \frac{[\eta:\mathcal{N}] = a}{\overline{\eta}\langle\zeta\rangle.P - \overline{aM} \to P} (INP) \frac{[\eta:\mathcal{N}] = a}{\eta(x).P - aM} \to P\{M/x\}$$

$$(SUM) \frac{P - \mu \to P'}{P + Q - \mu \to P'}$$

$$(REP) \frac{P|!P - \mu \to P'}{!P - \mu \to P'} (ALPH) \frac{Q - \mu \to Q' - P = a}{P - \mu \to Q'}$$

$$(PAR) \frac{P - \mu \to P'}{P + Q - \mu \to P'} if bn(\mu) \cap fn(Q) = 0$$

$$(RES) \frac{P - \mu \to P'}{(vc)P - \mu \to (vc)P'} if c \notin n(\mu)$$

$$(OPEN) \frac{P - (vc\overline{b})\overline{aM} \to P'}{(vc)P - (vc\overline{b})\overline{aM} \to P'} if n(M) \ni c \notin \{a, \overline{b}\}$$

$$(COM) \frac{P - aM \to P'}{P + Q - (vc\overline{b})\overline{aM} \to P'} if n(M) \ni c \notin \{a, \overline{b}\}$$

$$(GUARD) \frac{P - \mu \to P'}{\phi P - \mu \to P'} if \phi = t$$

$$(LET) \frac{P[\overline{\zeta}/z] - \mu \to P'}{|et z = \zeta in P - \mu \to P'} if \overline{\zeta} \neq 1$$

Sensitive-environment bisimulation is like a game of interactions between a process steps and the current environment's knowledge about names and keys. The moves of the process are constrained by this knowledge. This interaction can be ruled to be a proof technique for such systems under such environments. We need to model the steps taken by the environment as a reaction to corresponding steps triggered by the process. This can be implemented by building a function to map the reactions of the environment to corresponding actions of the process.

In order to define evade bisimulation, we have to precisely define when two environments represented by a pair of frame-theory (fr,th) with a pair of substitutions  $(\sigma, \rho)$  -( considered to have the same domain and constructed in the structure of (fr,th) pair )- can be considered as equivalent. Informally,

environments  $(fr, th)_{(\sigma, \rho)}$  and  $(fr', th')_{(\sigma', \rho')}$  are equivalent whenever they are logically two indistinguishable under this pair of substitutions. In other words, in order to compare the knowledge of environments, we need the environment behavior to be built into the frame-theory pair implemented by profiting from a pair of equivalent substitutions. Here, the frame is defined as a set of pairs of names (not like the original definition of Abadi and Gordon) considered to be known to the environments.

**Definition 5:** Let evade  $e = (fr, th)_{(\sigma, \rho)}$  be a frame-theory pair with a pair of equivalent substitutions  $(\sigma, \rho)$  such that  $\sigma \approx \rho$  (see Definition 7). A theory (th) is a finite subset of messages M X M indexed by using the projections  $\pi_i$  (th) and  $\pi_i$  (th) for i = 1, 2. A frame (fr) is a finite subset of names N X N known to the environments. We denote by E the set of all evades.

Defining a finite partial function that is used for mapping the set of names (considered as a domain) to the set of messages in the theory (considered as a proper co-domain), where the whole function is called substitution  $\sigma$ , i.e.  $\{M/x\}$ , for some  $M \in \mathcal{M} \in (th)_{\sigma}$  and  $x \in \mathcal{N}$  (variables).

**Definition 6:** Let the partial functions be as  $\sigma: x \to M$ ,  $\rho: x \to M$ , where  $dom(\sigma) = dom(\rho)$  then:  $1 - f(x) : x \rightarrow M X M$  and

 $2 - f(x): \sigma(x) \leftrightarrow \rho(x)$ , when  $\sigma(x) = \zeta \in M$  and  $\rho(x) = \eta \in M$ , then  $f(x): \zeta \leftrightarrow \eta$ .

To extend this definition to be defined in evade frame-theory pair with two equivalent substitutions, we have to determine the left and right position in th as a string  $\{l, r\} \in I$ , that is, a path through the nested pairs of  $\mathcal{M}$ .

**Definition 7:** let  $e = (fr, th)_{(\sigma,\rho)}$  be evade framed-theory pairs is consistent iff for all  $\zeta$  and  $\eta$  are messages, such that  $\left\{ \left( \underbrace{[\zeta_{l_i}:M]}_{n_i} \land \underbrace{[\eta_{r_i}:M]}_{n_i} \right) \mid (\zeta_{l_i}, \eta_{r_i}) \in (th)_{(\sigma,\rho)}, i = 1, 2 \right\}$  and using the projections with indexes i = 1, 2 such that  $\pi_{i}^{-1}\left(th_{(\sigma_{i}^{-1}+\rho_{i}^{-1})}\right) = \zeta$  and  $\pi_{i}^{-1}\left(th_{(\sigma_{i}^{-1}+\rho_{i}^{-1})}\right) = \eta$  to denote the left and right

position of the substitution pair corresponding to th. A frame is defined as a pair of names such that  $\left\{ \left( \underline{[a_{l_i}:N]} \land \underline{[b_{r_l}:N]} \right) | (a,b) \in fr$ ,  $i = 1, 2 \right\}$ , and a pair of substitutions  $(\sigma, \rho)$  considered equivalent

such that  $\sigma \approx \rho$ , when we have the following conditions:

 $i - \forall x_j, \sigma \text{ and } \rho$ , where  $dom(\sigma) \ni x_j \in dom(\sigma) \Rightarrow dom(\sigma) = dom(\rho) \text{ for } j = \{1, 2, ..., n\}$  and for  $\sigma: x_j \to \zeta$  and  $\rho: x_j \to \eta$  there is a partial function  $f(x_j): x_j \to \zeta$ ,  $\eta$ , such that  $f(x_j)=(th)(\sigma^{l}, \rho^{r})=(th)(\sigma^{l}, \rho^{r})$ 

$$\left\{ \left( \sigma^{l} \left( x_{j} \right), \rho^{r} \left( x_{j} \right) \right) \middle| \sigma^{l} \left( x_{j} \right) = \zeta \in \pi^{l}_{i} \left( th \right) \left( \sigma^{l}, \rho^{r} \right) \wedge \rho^{r} \left( x_{j} \right) = \eta \in \pi^{r}_{i} \left( th \right) \left( \sigma^{l}, \rho^{r} \right), \text{ for } i = 1, 2 \right\}$$

iii - if  $\sigma(x) \in N \Leftrightarrow \rho(x) \in N$ , where  $\sigma$  and  $\rho$  have the same domain  $x_j = (x_1, ..., x_n)$  $iv - if \zeta = Enc_k(\zeta') and \eta = Enc_l(\eta') then fr \cap \{k, l\} = \emptyset$ 

**Definition 8:** The synthesis S(.) of evade is defined as:  $S(e)_{(\sigma,\rho)} = S((fr, \emptyset), e)$ . We write  $e \succ \zeta \leftrightarrow \eta$  for  $(\zeta, \eta) \in S(e)$ ,  $e \not\succ \zeta \leftrightarrow \eta$  otherwise.

The next definition formalizes the synthesis S(.) of evade in the concept of maximal decryption depth of environments e, written dp(e). Elements in dp(e) represent the basic knowledge derivable from e, i.e. the "building blocks" the environment can use to synthesize more complex messages.

be a subset of M X M of messages, Definition 7. The maximal decryption depth  $(\sigma^{l}, \rho^{r})$ **Definition 9:** *let (th)* dn(th)  $(\ldots)$  can be derived by whitton

$$(Max - Dec - Depth) \frac{\left(Enc_{\mu_1}(\zeta_1), Enc_{\mu_2}(\zeta_2)\right) \in dp(th)}{(\zeta_1, \zeta_2) \in dp(th)} \quad (\mu_1, \mu_2) \in dp(th)}.$$

**Definition 10:** Let the knowledge of th, written as  $kn(th)_{(\sigma^l,\rho^r)}$ , be the set of names in  $dp(th)_{(\sigma^l,\rho^r)}$ , i.e.:  $kn(th)_{(\sigma^{l},\rho^{r})} := dp(th) \cap N \text{ and } \left\{ kn\left(\sigma^{l}\left(x_{j}\right)\right) = kn\left(\rho^{r}\left(x_{j}\right)\right) \left[ \left(\sigma^{l}\left(x_{j}\right),\rho^{r}\left(x_{j}\right)\right) \in th_{(\sigma^{l}_{j},\rho^{r}_{j})} \right] \right\} \text{ and the knowledge}$ of the environment e, written  $kn(e)_{(\sigma,\rho)}$  is defined as a set of names in  $kn(th)_{(\sigma^l,\rho^r)}$  and fr, i.e.:  $kn(e)_{(\sigma,\rho)} := (dp(th) \cup fr)_{(\sigma,\rho)} \cap N$ . In other word we can define the knowledge of the as:

$$kn (th)_{(\sigma^{1},\rho^{r})} := dp (th)_{(\sigma^{1},\rho^{r})} \left\{ \begin{array}{l} (Enc_{\mu 1} (\zeta_{1}), Enc_{\mu 2} (\zeta_{2})) \\ (\mu_{1},\mu_{2}) \in dp (th)_{(\sigma^{1},\rho^{r})} & \wedge (\zeta_{1},\zeta_{2}) \in M \end{array} \right\}$$

and the knowledge of e is:  $kn(e) := kn(th)_{(\sigma^{l}, \rho^{r})} \cup fr.$ 

Pairs of messages are decrypted using pairs of keys (names) considered equivalent by the environment This being the maximal decryption depth of evade theory. The resulting notion of knowledge kn(.) in fact preserves a minimal extension of the environment.

Note: From now, we will use the term non-decreasable function instead of knowledge of the environment kn(e), which means, no knowledge is disclosed any more to the environment.

**Definition 11:** From Definition 3, we can define a state,  $\left\{\sigma = \left\{\sigma_{\zeta_i^l}\right\}_{\zeta_i^l \in th} and \rho = \left\{\rho_{\zeta_i^r}\right\}_{\zeta_i^r \in th} | i = 1,2\right\}$ , to be a

family of multisets indexed by the terms  $\zeta_i^l$  and  $\zeta_i^r$ , where each  $\sigma_t$  represents the local state of the term t in  $\sigma$  and same for  $\rho$ , where  $(\zeta_i^l, \zeta_i^r) \in th_{(\sigma_i^l, \rho_i^r)}$ **Definition 12:** Let  $dp\left(e_{\pi_{t}^{l}(th)}^{\sigma}\right) := dp(range(\sigma))$  and  $kn\left(e_{\pi_{t}^{l}(th)}^{\sigma}\right) := kn(range(\sigma))$  same case for  $\rho$ .  $dp\left(e_{\pi_{i}^{l}(th)}^{\rho}\right) := dp\left(range\left(\rho\right) and kn\left(e_{\pi_{i}^{l}(th)}^{\rho}\right) := kn \left(range\left(\rho\right) for all i=1, 2.$ 

We introduce a function that decrypts a pair of messages  $(\zeta_1, \zeta_2)$  as far as possible, i.e.,  $(\zeta_1, \zeta_2) \in th$  assumed as a range of a pair of substitutions  $(\sigma, \rho)$ , using the knowledge of e and the pair of substitutions  $(\sigma, \rho)$ .

**Definition 13:** Let  $e = (fr, th)_{\sigma^{l}, \rho^{r}}$  be evade frame-theory pairs,  $(\zeta_{i}, \eta_{i}) \in th$  and given any equivalent pairs of substitutions  $(\sigma, \rho)$ , such that  $\sigma_{\pi_i^l(th)} \approx \rho_{\pi_i^r(th)}$ , if  $\sigma_{\pi_i^l(th)} = \begin{bmatrix} \zeta_j / \\ x_j \end{bmatrix}$ ,  $\rho_{\pi_i^r(th)} = \begin{bmatrix} \eta_j / \\ x_j \end{bmatrix}$ and  $i, j \in I$ , we denote by crux  $((\sigma, x_j), (\rho, x_j))$  what are left of  $(\zeta_j, \eta_j)$  after decrypting as much as pairs

possible using the keys in  $kn \left(\sigma^{l}(x_{i}) \cup \rho^{r}(x_{i})\right)$ . Formally, we define crux as:

$$\operatorname{crux}_{\left(\sigma_{\pi_{i}^{jl}(h)},\rho_{\pi_{i}^{jr}(h)}\right)}\left(\zeta_{j},\eta_{j}\right):=\begin{cases}\operatorname{crux}_{\left(\sigma_{\pi_{i}^{jl}(h)},\rho_{\pi_{i}^{jr}(h)}\right)}\left(\zeta_{j}',\eta_{j}'\right) \text{ if } \zeta_{j}=\operatorname{Enc}_{k}\left(\zeta_{j}'\right), \eta_{j}=\operatorname{Enc}_{l}\left(\eta_{j}'\right) \right)\\ \text{ and } fr \neq (k,l) \in \operatorname{kn}\left(\left(\sigma_{\pi_{i}^{jl}(h)}\right) \cup \left(\rho_{\pi_{i}^{jr}(h)}\right)\right)\\ \left(\zeta_{j},\eta_{j}\right) \text{ otherwise.}\end{cases}$$

**Definition 14:** We decompose any pair of messages  $(\zeta, \eta) \in th$  with a pair of equivalent substitutions  $(\sigma, \rho)$  such that  $\sigma \sim \rho$  into:  $[(\zeta\sigma), (\eta\rho)] = \left( Enc_{k_{n}} \left( \dots \left( Enc_{k_{2}} \left( Enc_{k_{1}} (crux (\zeta)) \right) \right) \dots \right), Enc_{l_{n}} \left( \dots \left( Enc_{l_{2}} \left( Enc_{l_{1}} (crux (\eta)) \right) \dots \right) \right) \right) \right) \text{for } (\zeta, \eta) \in th_{[\sigma^{l}, \rho^{r}]}$ and any equivalent pair of substitutions  $(\sigma, \rho)$  with  $\{k_1, ..., k_n\} \subseteq kn\left(e_{\pi_i^l(th)}^{\sigma}\right)$  and  $\{l_1, ..., l_n\} \subseteq kn\left(e_{\pi_i^r(th)}^{\rho}\right)$ , if  $crux_{\left(\sigma_{\pi_i^l(th)}^{\rho}, \sigma_{\pi_i^r(th)}^{r}\right)}(\zeta, \eta) = \left(Enc_k(\zeta'), Enc_l(\eta')\right)$ , then we have  $fr \not i (k, l) \in kn \left( \left( e^{\rho}_{\pi_{1}^{r}(th)} \right) \cup \left( e^{\rho}_{\pi_{1}^{r}(th)} \right) \right)$ . As a special case,

$$\operatorname{crux} \left( \left( \sigma_{\pi_{i}}^{l}(th), x_{j}^{r} \right), \left( \rho_{\pi_{i}}^{r}(th), x_{j}^{r} \right) \right) = \operatorname{crux} \left( \sigma^{l}(x_{j}), \rho^{r}(x_{j}) \right).$$
 Therefore,  

$$\operatorname{kn} \left( \left( \sigma_{\pi_{i}}^{l}(th) \right) \cup \left( \rho_{\pi_{i}}^{r}(th) \right) \right) = \left\{ \operatorname{crux} \left( \left( \sigma_{\pi_{i}}^{l}(th), x_{j}^{r} \right), \left( \rho_{\pi_{i}}^{r}(th), x_{j}^{r} \right) \right) \mid \operatorname{dom} (\sigma) \not \ni x_{j} \notin \operatorname{dom} (\rho) \right\}$$

$$\text{The environment } \rho = \left( \operatorname{fr}(th) \right) = \left\{ \operatorname{crux} \left( \left( \sigma_{\pi_{i}}^{l}(th), x_{j}^{r} \right), \left( \rho_{\pi_{i}}^{r}(th), x_{j}^{r} \right) \right) \mid \operatorname{dom} (\sigma) \not \ni x_{j} \notin \operatorname{dom} (\rho) \right\}$$

The environment  $e = (fr, th)_{(\sigma^l, \rho^r)}$  pairs that only contains pairs of messages, is consistent if the

attacker cannot distinguish between the messages in  $\pi_i^l(th)$ :  $\sigma^l(x_j)$  and their counterparts in  $\pi_i^r(th)$ :  $\sigma^r(x_j)$  for all i = 1, 2 and  $i \in I$ .

$$\pi_i^r(th): \rho^r(x_j), \text{ for all } i=1, 2 \text{ and } j \in I$$

The attacker can:

- 1- distinguish between names and encrypted messages,
- 2- ascertain equality of messages and
- 3- attempt decryption of messages with a key of his own making.

To show the equivalence of the consistent *evade* pairs with consistent pairs of substitutions. We can use the crux to get an *evade* as follows:

Note, we will use a short-hand C(.) for crux(.).

**Definition 15:** let 
$$e = (fr, th)_{(\sigma^l, \rho^r)} \succ ok$$
 be an evade frame-theory pair considered consistent with the

equivalent pairs of substitutions  $(\sigma, \rho)$ , such that  $\sigma \sim \rho$ , whenever  $\sigma$  and  $\rho$  have the same domain  $x_i = \{x_1, ..., x_n\}$  and for all i = 1, 2. The following conditions hold:

$$\begin{split} I - \forall x_{j}, dom(\sigma) \ni x_{j} \in dom(\rho), \exists \zeta, \eta : [\zeta^{l} : M]^{h} [\eta^{r} : M]; \text{ where } n(\zeta^{l}) \in dom(\sigma) \\ & \text{then } [\zeta^{l} \sigma_{j}^{l}] = C(\sigma_{j}^{l}, x_{j}) \text{ and } [\eta^{r} \rho_{j}^{r}] = C(\rho_{j}^{r}, x_{j}) \\ 2 - (\sigma_{j}^{l}(x_{j}), \rho_{j}^{r}(x_{j})) \in \text{ th }, \text{ if } \sigma_{j}^{l}(x_{j}) = \zeta \text{ and } \rho_{j}^{r}(x_{j}) = \eta \text{ then } e \succ \zeta \leftrightarrow \eta \Rightarrow e \succ \sigma_{\pi_{1}^{l}(h)}^{\gamma} \rho_{\pi_{1}^{r}(h)} \\ 3 - C(\sigma_{j}^{l}(x_{j})) \in N \Leftrightarrow C(\rho_{j}^{r}(x_{j})) \in N \\ 4 - C(\sigma_{j}^{l}(x_{j})) = C(\sigma_{n}^{l}(x_{n})) \Leftrightarrow C(\rho_{j}^{r}(x_{j})) = C(\rho_{n}^{r}(x_{n})) \\ 5 - \text{ for } \sigma_{\pi_{1}^{l}(h)}^{\gamma} \sim \rho_{\pi_{1}^{r}(h)} \text{ where } dom(\sigma) = x_{j} = dom(\rho), \text{ we let } (\zeta_{j}^{l}, \eta_{j}^{r}) \in \text{ th } (\sigma_{j}^{l}, \rho_{j}^{r}); \zeta_{j}^{l} = C(\sigma_{j}^{l}, x_{j}) \\ and \eta_{j}^{r} = C(\rho_{j}^{r}, x_{j}) \text{ Then form that and } l, 2, \text{ we have either :} \\ a) [\zeta_{j}^{l} \sigma_{j}^{l}] = [\eta_{j}^{r} \rho_{j}^{r}] = \bot \text{ or } \\ b) \text{ There are } j \text{ and } a \text{ tuple } \tilde{\iota} \text{ of indices from } I \text{ such that } : \\ [\zeta_{j}^{l} \sigma_{j}^{l}] = Enc_{\zeta_{j}^{l}} (\dots Enc_{\zeta_{j}^{l}} (\dots Enc_{\zeta_{j}^{l}} (\zeta_{j}^{l})) \dots ] \\ [\eta_{j}^{r} \rho_{j}^{r}] = Enc_{\eta_{j}^{r}} (m_{j}^{r} (\dots Enc_{\eta_{j}^{r}} (\eta_{j}^{r})) \dots ] \\ [\eta_{j}^{r} (\rho_{j}^{r}), \rho_{j}^{r}(x_{j})) \in \text{ th then we have} \end{split}$$

$$\sigma_{j}^{l}(x_{j}) = Enc C\left(\sigma_{j}^{l}, x_{j_{m}}\right) \left( \dots Enc C\left(\sigma_{j}^{l}, x_{j_{2}}\right) \left( Enc C\left(\sigma_{j}^{l}, x_{j}\right) \left( C\left(\sigma_{j}^{l}, x_{j}\right) \right) \right) \dots \right),$$

$$\rho_{j}^{r}(x_{j}) = Enc C\left(\rho_{j}^{r}, x_{j_{m}}\right) \left( \dots Enc C\left(\rho_{j}^{r}, x_{j_{2}}\right) \left( Enc C\left(\rho_{j}^{r}, x_{j}\right) \left( C\left(\rho_{j}^{r}, x_{j}\right) \right) \right) \dots \right),$$

$$Parameter 1 = Let enc C\left(\rho_{j}^{r}, x_{j_{m}}\right) \left( \dots Enc C\left(\rho_{j}^{r}, x_{j_{2}}\right) \left( Enc C\left(\rho_{j}^{r}, x_{j}\right) \left( C\left(\rho_{j}^{r}, x_{j}\right) \right) \right) \dots \right),$$

$$Parameter 1 = Let enc C\left(\rho_{j}^{r}, x_{j_{m}}\right) \left( \dots Enc C\left(\rho_{j}^{r}, x_{j_{m}}\right) \left( Enc C\left(\rho_{j}^{r}, x_{j}\right) \left( Enc C\left(\rho_{j}^{r}, x_{j}\right) \right) \right) \dots \right),$$

**Example 1:** let  $e = (fr, th) (\sigma^l, \rho^r) \succ ok$  be an evade frame-theory pair considered consistent with an

equivalent pair of substitutions  $(\sigma, \rho)$ , as in the previous Definition, and we have the following:

$$\pi_{i}^{l}(th)^{\sigma} = \left\{ \left( (Enc_{k} \{\zeta_{1}\}/x_{1}), (Enc_{g} \{\eta_{1}\}/x_{2}) \right) \right\}$$
Then we have:  
$$\pi_{i}^{r}(th)^{\rho} = \left\{ \left( (Enc_{k} \{\zeta_{2}\}/x_{1}), (Enc_{g} \{\eta_{2}\}/x_{2}) \right) \right\}$$
Then we have:  
$$(th)_{(\sigma^{l},\rho^{r})} = \left\{ \left( (Enc_{k} \{\zeta_{1}\}/x_{1}), (Enc_{k} \{\zeta_{2}\}/x_{1}) \right), ((Enc_{g} \{\eta_{1}\}/x_{2}), (Enc_{g} \{\eta_{2}\}/x_{2})) \right) \right\}$$
and  $\pi_{i}^{l}(th)^{\sigma} \approx \pi_{i}^{l}(th)^{\rho}.$ 

To compare the knowledge of environments we use the following pre-order:

**Definition 16:** let  $e = (fr, th) \begin{pmatrix} \sigma^{l}, \rho^{r} \end{pmatrix}$  and  $e' = (fr', th')_{(\sigma^{l}, \rho^{r})}$ , e' extends e written as  $e \le e'$  if and only if

 $dp\left(e_{(\sigma^{l},\rho^{r})}\right) \subseteq dp\left(e_{(\sigma^{l},\rho^{r})}\right)$ . Two evade frame-theory pairs e and e' with consistent pairs of substitution such that  $\sigma \approx \rho$  are assumed  $\mathcal{M}$ -equivalent, written  $(fr,th)_{(\sigma^{l},\rho^{r})} \triangleleft \triangleright (fr',th')_{(\sigma^{l},\rho^{r})}$  if  $e \triangleleft \triangleright e'$ ,  $e' \triangleleft \triangleright e$  and when

kn(e) = kn(e'). Then  $\triangleleft \triangleright$  is transitive and reflexive by the same properties for  $\subseteq$ . For results on antisymmetry, the following example and Corollary 21 are used:

**Example 2:** let  $e_1 = \{ \{(ch, ch), (\eta, \mu, g)\}, ((Enc_{\mu}(\zeta), Enc_{g}(\zeta'))) \}$  and  $e_2 = \{ \{(ch, ch), (\eta, \mu, g)\}, ((Enc_{\mu}(\zeta), Enc_{\zeta}(Enc_{g}(\zeta')))) \}$  then  $e_1 \triangleleft \triangleright e_2$ . Generally, if e is evade,  $e_1 \leq e$  and  $e_2 \leq e$  then  $e \cup e_1 \triangleleft \triangleright e \cup e_2$ .

Lemma 17:  $e' \leq e$  iff  $e' \subseteq S(e)$ 

**Proof:**  $e' \leq e \implies e' \subseteq dp(e)$ , since  $e' \subseteq dp(e') \subseteq dp(e)$ .

To show the other implication, assume that  $e' \subseteq dp(e)$  and take any  $(\zeta, \eta) \in th'_{(\sigma^{l}, \rho^{r})}$  such that  $e'_{(\sigma^{l}, \rho^{r})} \succ \sigma^{l}(x_{j}) \leftrightarrow \rho^{r}(x_{j})$  where  $\pi_{i}^{l}(th') = \zeta = \sigma^{l}(x_{j})$  and  $\pi_{i}^{r}(th') = \eta = \rho^{r}(x_{j})$  for all i = 1,2 and  $x_{j} = \{x_{l}, ..., x_{n}\}$  we have  $\sigma_{(th)} \approx \sigma_{(th')}, \rho_{(th)} \approx \rho_{(th')}, \sigma_{(th)} \approx \rho_{(th)} \Rightarrow \sigma_{(th')} \approx \rho_{(th')}$  where all have the same domain  $x_{j}$ . We show that  $e_{(\sigma, \rho)} \succ \sigma(x) \leftrightarrow \rho(x)$  by induction on the derivation of  $e'_{(\sigma', \rho')} \succ \sigma'(x) \leftrightarrow \rho'(x)$ . If  $(\zeta, \eta) \in th'_{(\sigma^{l}, \rho^{r})}$  then  $e'_{(\sigma^{l}, \rho^{r})} \succ \sigma^{l}(x_{j}) \leftrightarrow \rho^{r}(x_{j})$  by the assumption. Else, by the assumption of *Max-Dec-Depth*, there are  $\zeta', \eta', \mu, g$  such that  $\zeta = \text{Enc}_{\mu}(\zeta')$  and  $\eta = \text{Enc}_{g}(\eta')$ . By the induction hypothesis  $e \succ \zeta' \leftrightarrow \eta'$  and  $e \succ \mu \leftrightarrow g$ .

An evade process pair is a triple ((e), P, Q) where  $e = (fr, th)(\sigma^{l}, \rho^{r})$ , fr is a frame, th is a theory evaluated under a pair of substitutions  $(\sigma^{l}, \rho^{r})$  indexed by  $\{l, r\}$  where  $dom(\sigma) = dom(\rho)$  and P and Q are processes. An evade relation R is a set of evade process pairs. We write  $e \succ P R Q$  if  $((e), P, Q) \in R R$  is consistent if e is consistent whenever  $e \succ P R Q$ .

Now we have got enough notations to define evade bisimilarity.

**Definition 18:** A consistent evade relation R is an evade simulation if whenever:

 $e \succ P \ R \ Q \ and \ P \xrightarrow{\mu_1} P' \Rightarrow Q \xrightarrow{\mu_2} Q' \ with$   $a) \ bn(\mu_1) \cap n\left(\pi_i^l(th) \left(\sigma^l, \rho^r\right)\right) \cap n\left(\pi_i^l(fr)\right) = \emptyset = bn(\mu_2) n\left(\pi_i^r(th) \left(\sigma^l, \rho^r\right)\right) \cap n\left(\pi_i^r(fr)\right), for \ i=1,2 \ (bound names are \ fresh)$   $b) \left[\underline{\sigma(ch(\mu_1))}\right] \in \pi_i^l(fr) \land \underline{[\rho(ch(\mu_2))]} \in \pi_i^r(fr) \ for \ dom(\sigma) = \ dom(\rho), fn(\mu_1, \mu_2) \subseteq \ dom(\sigma) \ (the \ transitions \ are \ detected)$  then

 $l-if \mu_1 = \tau$  then  $\mu_2 = \tau$  and  $e \succ P' RQ'$ .

 $2 - if \ \mu_1 = ch_1(x_1) \ and \ there \ are \ \zeta_1, \eta_1 \ such \ that(\eta_1 \sigma) = ch_1 \in \pi_i^l(fr), \ (\zeta_1 \sigma) = M_1 \ and \ [\eta_1 : \mathcal{N}], \ [\zeta_1 : \mathcal{M}] \in \pi_i^l(th)(\sigma^{-1}, \rho^{-r}), \ then \ there \ model{eq:substance}$   $exists \ \mu_2 = ch_2(x_2) \ with \ \zeta_2, \eta_2 \ such \ that(\eta_2 \rho) = ch_2 \in \pi_i^r(fr), \ (\zeta_2 \rho) = M_2 \ and \ [\eta_2 : \mathcal{N}],$ 

 $[\zeta_2: M] \in \pi_i^r(th)(\sigma_{\rho}^r)$  and for all  $B, \zeta_1, \zeta_2$  with  $B \subset N \times N$  consistent and

- $-\pi_{1}(B) \mid n(\zeta_{1}) = \emptyset = \pi_{2}(B) \mid n(\zeta_{2})$  (all new names are needed)
- $-\pi_{1}(B) \cap (fn(P) \cup n(\pi_{i}^{l}(th)_{(\sigma^{l},\rho^{r})})) \cup \pi_{i}^{l}(fr) = \emptyset = \pi_{2}(B) \cap (fn(Q) \cup n(\pi_{i}^{r}(th)_{(\sigma^{l},\rho^{r})})) \cup \pi_{i}^{r}(fr))$ (new names are fresh)

 $-(fr \cup B, th) \succ \zeta_{1} \leftrightarrow \zeta_{2} \ (\zeta_{1} \ and \ \zeta_{2} \ are \ indistingu \ ishable) \ we \ have \ \left((fr \cup B, th) \ (\sigma, \rho)\right) \succ P'\left[\zeta_{1}/\chi_{1}\right] R \ Q'\left[\zeta_{2}/\chi_{2}\right].$   $3 - if \ \mu_{1} = \left(v \ \tilde{c}_{1}\right) \overline{ch}_{1} \ \zeta_{1} \ and \ there \ is \ \eta_{1} \ such \ that \ fn \ (\eta_{1}) \subseteq \ dom \ (\sigma) \ and \ \left(\underline{\eta_{1}\sigma}\right) = ch_{1} \in \pi_{i}^{1}(fr) \ and \ \underline{[\eta_{1}:\mathcal{N}]}, \ \underline{[\zeta_{1}:\mathcal{M}]} \in \pi_{i}^{1}(th)(\sigma^{1},\rho^{r}) \ and \ \{\tilde{c}\}_{1} \cap \left(fn \ (P) \cup n \ (\pi_{i}^{1}(th)(\sigma^{1},\rho^{r}) \cup \pi_{i}^{1}(fr))\right) = \emptyset \ then \ there \ exists$   $\mu_{2} = \left(v \ \tilde{c}_{2}\right) \overline{ch} \ 2 \ \zeta_{2} \ and \ there \ is \ \eta_{2} \ such \ that \ fn \ (\eta_{2}) \subseteq \ dom \ (\sigma \ ) \ and \ (\eta_{2}\rho) = \overline{ch}_{2} \in \pi_{i}^{r} \ (fr), \ \underline{[\eta_{2}:\mathcal{N}]}, \ \underline{[\zeta_{2}:\mathcal{M}]} \in \pi_{i}^{r}(th)(\sigma^{1},\rho^{r}) \ and \ \{\tilde{c}_{2}\} \cap \left(fn \ (Q) \cup n \ (\pi_{i}^{r}(th)(\sigma^{1},\rho^{r})) \cup \pi_{i}^{r} \ (fr)) = \emptyset. \ Then \ we \ have : \ \overline{kn \ e \cup} \ (fr, th)(\sigma^{1},\rho^{r})\} \succ P' \ R \ Q'.$ 

In the above definition, channel correspondence is checked by adding the channels to the *fr* considered to be known by the environment. If there is no correspondence between  $(ch(\pi_1(fr)) \nleftrightarrow ch(\pi_2(fr)))$ , the resulting environment will not be consistent.

On process output we use  $kn(\cdot)$  to construct the new environment after the transitions. This necessitates applying all decryptions with keys that are known by the environment, producing the minimal extension of the environment e with  $(fr,th)(fr,th)(\sigma^{l},\rho^{r})$  for  $(\zeta_{1},\zeta_{2}) \in th$  and  $dom(\sigma) = dom(\rho)$ .

On process input, any input that the environment can construct (i.e., satisfying  $(fr \cup B, th) \succ \zeta_1 \leftrightarrow \zeta_2$ must be considered. Automating bisimilarity checks is thus made difficult, since the set of potential inputs is infinite. However, due to the large number of inputs to consider, this method is practical only for finite processes. But here we showed that evade bisimilarity is decidable for finite processes (large number of inputs, but not infinite).

**Definition 19:** S is an evade bisimulation if both S and  $S^{-1}$  are evade simulations.

**Definition 20:** An evade bisimilarity is the greatest evade bisimulation, written  $\approx_e$ , which is the union of all evade bisimulations ( $\approx_e$  is symmetric).

#### 7.3 PROVES AND PROPERTIES OF EVADE BISIMULATION:

Here, we will give some Lemmas proving our technique, and the main properties of preorder relation. Corollary 21: Some properties relating  $\leq$  with some operations:

1- If  $e' \subseteq e$  then  $e' \leq e$ .

 $2 - If e'_1 \le e \text{ and } e'_2 \le e \text{ then } (e'_1 \cup e'_2) \le e.$ 

 $3 - If e'_1 \le e_1 \text{ and } e'_2 \le e_2 \text{ then } \left(e'_1 \cup e'_2\right) \le \left(e_1 \cup e_2\right).$ 

The two  $\mathcal{M}$ -equivalent e and e' preserved by Kn(.) are equal, so the preorder  $\leq$  is an ordering relation on the set of them.

**Lemma 22:** If  $e \triangleleft e'$ , then  $Kn(e) \leq Kn(e')$ .

From the Definitions 16 and 17 we have:

**Definition 23:** *Evade is non-decreasable if* e = kn (e). *e is decreasable if e is not non-decreasable.* An alternative definition is as follows:

Lemma 24: An evade e is non-decreasable iff the following condition holds:

 $If(Enc_{k}(\zeta), Enc_{g}(\eta)) \in th_{(\sigma^{l}, \rho^{r})} then(k, g) \notin th_{(\sigma^{l}, \rho^{r})}, where \quad \pi_{i}^{l}(th_{(\sigma^{l}, \rho^{r})}) = \sigma^{l}(x), \pi_{i}^{r}(th_{(\sigma^{l}, \rho^{r})}) = \rho^{r}(x) \quad and \quad dom(\sigma^{l}) = dom(\rho^{r}), \text{ for } i = 1, 2.$ 

**Proof:** if this holds then we cannot apply *Max-Dec-Depth* to any pair in  $th_{(\sigma^{l},\rho^{r})}$  with an equivalent pair of substitutions, so  $dp(th)_{(\sigma^{l},\rho^{r})} = th_{(\sigma^{l},\rho^{r})}$ . By the definition of  $kn(th)_{(\sigma^{l},\rho^{r})}$  we then have that  $kn(th)_{(\sigma^{l},\rho^{r})} = th_{(\sigma^{l},\rho^{r})}$ . If  $th_{(\sigma^{l},\rho^{r})}$  is non-decreasable then the disjointedness holds by the definition of  $kn(th)_{(\sigma^{l},\rho^{r})}$ , using that  $dp(th)_{(\sigma^{l},\rho^{r})} \supseteq kn(th)_{(\sigma^{l},\rho^{r})}$ .

**Corollary 25:**  $kn(th)_{(\sigma^t, \sigma^r)}$  is non-decreasable for all evades *th*.

As might be expected, the non-decreasable function of evade can be used to generate any message that can be generated by the hedge.

Lemma 26: For any evade  $e, e \leq dp(e)_{(\sigma^{l},\rho^{r})} \leq kn(e)_{(\sigma^{l},\rho^{r})}$ . **Proof:** As  $e \subseteq dp(e)_{(\sigma^{l},\rho^{r})} \supseteq kn(e)_{(\sigma^{l},\rho^{r})}$  Corollary 21 gives that  $e \leq dp(e)_{(\sigma^{l},\rho^{r})} \ge kn(e)_{(\sigma^{l},\rho^{r})}$ . What remains to be proved is  $dp(e)_{(\sigma^{l},\rho^{r})} \ge kn(e)_{(\sigma^{l},\rho^{r})}$ . By Lemma 17, it suffices to show  $dp(e)_{(\sigma^{l},\rho^{r})} \subseteq S(kn(e)_{(\sigma^{l},\rho^{r})})$ . Assume that  $(\zeta,\eta) \in kn(e)_{(\sigma^{l},\rho^{r})}$ , we show that  $kn(e) \succ \zeta \leftrightarrow \eta$  by structural induction on  $\zeta$ . If  $\zeta \in N$  then  $(\zeta,\eta) \in kn(e)_{(\sigma^{l},\rho^{r})}$ . Otherwise there are  $\zeta'$  and k such that  $\zeta = Enc_{k}(\zeta')$ . If  $(\zeta,\eta) \in kn(e)_{(\sigma^{l},\rho^{r})}$  otherwise, by definition of kn (.) there are  $\eta'$  and g such that  $\eta = Enc_{g}(\eta'), (\zeta',\eta') \in dp(e)_{(\sigma^{l},\rho^{r})}$  and  $(k,g) \in dp(e)_{(\sigma^{l},\rho^{r})}$ . By the induction hypothesis we have  $kn(e)_{(\sigma,\rho)} \succ \zeta \leftrightarrow \eta$ .

Non-decreasable evade is a subset of any M –equivalent evade. **Lemma 27:** *if*  $e' \triangleleft \triangleright e$  and e' *is* non–decreasable then  $e' \subseteq e$ . **Proof:** Having any  $(\zeta, \eta) \in (\text{th}')_{(\sigma'^{l}, \sigma'^{-r})}$ . As  $e' \triangleleft \triangleright e, e \succ \zeta \leftrightarrow \eta$ . We have two cases: - If  $\zeta \in \mathcal{N}$  or  $\eta \in \mathcal{N}$  then  $(\zeta, \eta) \in (\text{th}')_{(\sigma'^{l}, \sigma'^{-r})}$  by Definition 7- (iii).

- Else,  $\zeta = Enc_k(\zeta')$  and  $\eta = Enc_g(\eta')$ . Since e' is non-decreasable  $(k,g) \notin e'$  by Lemma 24. By Definition 7- (iii)  $e' \neq k \leftrightarrow g$ , so  $e \neq k \leftrightarrow g$  and *Max-Dec-Depth* cannot derive  $e \succ \zeta \leftrightarrow \eta$ . This shows that  $(\zeta, \eta) \in e$ .

Two M-equivalent non-decreasable evades are equal, so the preorder is  $\leq$  an ordering relation in the set of non-decreasable evades.

**Corollary 28:** If  $(e)_{(\sigma^{l},\rho^{r})} \leq (e')_{(\sigma^{l},\rho^{r})}$  and both *e* and *e'* are non-decreasable preserved by *Kn*(.), then e = e'.

The ordering of evades is preserved by kn(.). Lemma 29: If  $e' \le e$ , then  $kn(e')_{(\sigma',\rho'')} \le kn(e)_{(\sigma',\rho'')}$ .

**Proof:** from Lemma  $26 \ln(e')_{(\sigma'^{I},\rho'^{r})} \leq dp(e)_{(\sigma^{I},\rho^{r})}$ , so by the transitivity of  $\leq$  we only need to show  $dp(e')_{(\sigma'^{I},\rho'^{r})} \leq ln(e)_{(\sigma^{I},\rho')}$ . By Lemma 17 this holds iff  $dp(e') \subseteq S(\ln(e))$ , which we show by induction on the derivation of  $dp(e')_{(\sigma'^{I},\rho'^{r})}$ . Take  $any(\zeta,\eta) \in dp(e')_{(\sigma'^{I},\rho'^{r})}$ , the base case is that  $(\zeta,\eta) \in (e')_{(\sigma'^{I},\rho'^{r})}$ . By Lemma 26  $(e)_{(\sigma^{I},\rho^{r})} \leq ln(e)_{(\sigma^{I},\rho'^{r})}$ , so  $(e')_{(\sigma'^{I},\rho'^{r})} \leq ln(e)_{(\sigma^{I},\rho'^{r})}$  by the transitive of  $\leq$ . In particular,  $ln(e) \succ \zeta \leftrightarrow \eta$ . Otherwise we have to use Max-Dec-Depth to derive  $(\zeta,\eta) \in dp(e')_{(\sigma'^{I},\rho'^{r})}$  which means that there are k and g such that  $(\text{Enc}_{k}(\zeta), \text{Enc}_{g}(\eta)) \in dp(th')_{(\sigma'^{I},\rho'^{r})}$  and  $(k,g) \in dp(e')_{(\sigma'^{I},\rho'^{r})}$ . By induction  $ln(e)_{(\sigma^{I},\rho^{r})} \succ Enc_{k}(\zeta) \leftrightarrow Enc_{g}(\eta)$  and  $ln(e)_{(\sigma^{I},\rho^{r})} \succ k \leftrightarrow g$ . By Definition 7- (iii)  $(k,g) \in ln(e)_{(\sigma^{I},\rho^{r})}$ , so  $(Enc_{k}(\zeta), Enc_{g}(\eta)) \notin ln(th')_{(\sigma'^{I},\rho'^{r})}$  by the definition of ln(.). Then Max-Dec-Depth must have been used to derive  $ln(e)_{(\sigma^{I},\rho^{r})} \succ Enc_{k}(\zeta) \leftrightarrow Enc_{g}(\eta)$ , which gives that  $ln(e)_{(\sigma^{I},\rho^{r})} \succ \zeta \leftrightarrow \eta$ .

The non-decreasable of two M-equivalent evades are equal. **Lemma 30:** *if*  $(e')_{(\sigma'^{l},\rho'^{r})} \triangleleft (e)_{(\sigma^{l},\rho')}$ , *then*  $kn(e')_{(\sigma'^{l},\rho'^{r})} = kn(e)_{(\sigma^{l},\rho')}$ . *Proof:*  $kn(e')_{(\sigma'^{l},\rho'^{r})} \triangleleft (kn(e)_{(\sigma^{l},\rho')})$  by Lemma 7.3.9.  $kn(e')_{(\sigma'^{l},\rho'^{r})}$  and  $kn(e)_{(\sigma^{l},\rho'^{r})}$  are both nondecreasable by Corollary 25. The equality then follows from Corollary 28. **Lemma 31:** *If* e' *and* e *are evades, then*  $kn(kn(e)_{(\sigma^{l},\rho'^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}) = kn((e)_{(\sigma^{l},\rho'^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})})$ . **Proof:** By Corollary 21-(1)  $(e')_{(\sigma'^{l},\rho'^{r})} \leq \left(\left(e\right)_{(\sigma^{l},\rho^{r})} \cup \left(e'\right)_{(\sigma'^{l},\rho'^{r})}\right)$ , so using Lemma 29 we have that  $kn((e')_{(\sigma,\rho)}) \leq kn((e)_{(\sigma^{l},\rho^{r})} \cup (e')_{(\sigma,\rho)})$ . By Lemma 26  $(e')_{(\sigma'^{l},\rho'^{r})} \leq kn((e')_{(\sigma'^{l},\rho'^{r})})$ , so by transitivity  $(e')_{(\sigma'^{l},\rho'^{r})} \leq kn((e)_{(\sigma^{l},\rho^{r})} \cup (e')_{(\sigma'^{l},\rho'^{r})})$ . Concerning  $kn((e)_{(\sigma^{l},\rho^{r})})$ , note that  $kn((e)_{(\sigma^{l},\rho^{r})}) \equiv dp((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}) \leq kn((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})})$ , where the last relation is due to Lemma 17. By Corollary 21-(2) $\left(kn((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}\right) \leq kn\left((e)_{(\sigma^{l},\rho^{r})}\right) \cup (e')_{(\sigma'^{l},\rho'^{r})}) \leq kn\left((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}\right)$ .  $(e)_{(\sigma^{l},\rho^{r})} \leq kn\left((e)_{(\sigma^{l},\rho^{r})}\right) \cup (e')_{(\sigma'^{l},\rho'^{r})}$ , so by Lemma 26, so by Corollary 21-(3) we have that  $\left((e)_{(\sigma^{l},\rho^{r})} \cup (e')_{(\sigma'^{l},\rho'^{r})}\right) \leq kn\left(kn((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}\right)$  and  $\left(kn((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}\right) \leq kn\left(kn((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}\right)$ . By Lemma 29 we have that  $kn\left((e)_{(\sigma^{l},\rho^{r})} \cup (e')_{(\sigma'^{l},\rho'^{r})}\right) \leq kn\left(kn((e)_{(\sigma^{l},\rho^{r})}) \cup (e')_{(\sigma'^{l},\rho'^{r})}\right)$ . The equality follows from Corollary 28.

From what we have seen so far, an environment mapping should preserve consistency. To prove that this holds for the environment mappings we will define, we then investigate consistent evades and their properties.

Lemma 32: If *e* is consistent then *e* is non-decreasable.

**Proof:** By Definition 7 for consistency, we have that  $((Enc_k(\zeta)), (Enc_g(\eta))) \in (th)_{(\sigma^l, \rho^r)}$  implies  $(k, g) \notin (fr)_{(\sigma^l, \rho^r)}$ . By Lemma 24 this means that *e* is non-decreasable.

Note that we have only used a special case of Definition 7 in the proof of Lemma 32. The all conditions for consistency are pairwise disjointed, so consistency is a much stronger constraint than non-decreasability.

For consistency a generalized version of Definition 7 is that a consistent *evades* cannot generate two message pairs that only differ in one component.

**Lemma 33:** Let *e* be consistent *evade* with  $e \succ \zeta \leftrightarrow \eta$  and  $e \succ \zeta' \leftrightarrow \eta'$ . Then  $\zeta = \zeta'$  *iff*  $\eta = \eta'$ .

**Proof:** By symmetry we need only to argue the case  $\zeta = \zeta'$ . The proof is by induction on the derivation of  $e \succ \zeta \leftrightarrow \eta$ . If  $(\zeta, \eta) \in (th)_{(\sigma^l, \rho^r)}$  we will first show that  $(\zeta, \eta') \in (th)_{(\sigma^l, \rho^r)}$ . If  $\zeta$  is a name this follows from Definition 7. Otherwise  $\zeta = Enc_k(M)$ , but since  $k \notin \pi_1^l(th)_{(\sigma^l, \rho^r)}$  by Definition 7 of consistency we cannot use *Max-Dec-Depth* to derive  $e \succ \zeta \leftrightarrow \eta'$ . Now, we know that  $(\zeta, \eta) \in (th)_{(\sigma^l, \rho^r)}$  and  $(\zeta, \eta') \in (th)_{(\sigma^l, \rho^r)}$ , when  $dom(\sigma^l) = dom(\rho^r)$  then  $\eta = \eta'$  by Definition 7 for consistency. If  $\zeta = Enc_k(M)$ ,  $\eta = Enc_g(N)$ ,  $e \succ M \leftrightarrow N$  and  $e \succ k \leftrightarrow g$  then  $k \in \pi_1^l(th)_{(\sigma^l, \rho^r)}$  by Definition 7. As *e* is consistent,  $\zeta \notin \pi_1^l(th)_{(\sigma^l, \rho^r)}$ , so we must have used *Max-Dec-Depth* to derive  $e \succ \zeta \leftrightarrow \eta'$ . This gives that  $\eta' = Enc_a(N')$  for some *a*, *N'* such that  $e \succ M \leftrightarrow N'$  and  $e \succ k \leftrightarrow a$ . By induction N = N' and g = a.

Two M-equivalent consistent evades are always equal.

**Lemma 34:** If  $e' \triangleleft \triangleright e$  and both e' and e are consistent, then e' = e.

**Proof:** e' and e are non-decreasable by Lemma 32. The equality follows from Corollary 28.

Any non-decreasable of a consistent evade is consistent.

**Lemma 35:** If e is consistent, e' is non-decreasable and  $e' \leq e$  then e' is consistent.

**Proof:** Assume that  $(\zeta, \eta) \in (th')_{(\sigma'^{l}, \rho'^{r})}$  and note that  $e \succ \zeta \leftrightarrow \eta$  when  $\zeta = \sigma'^{l}(x)$  and  $\eta = \rho'^{r}(x)$ . We only need to show one direction of the symmetric conditions.

1. If  $\zeta \in N$  then  $(\zeta, \eta) \in (th)_{(\sigma^{l}, \rho^{r})}$  by Definition 7, so  $\eta \in \mathcal{N}$  as *e* is consistent.

- 2. See Lemma 33.
- 3. Assume that  $\zeta = Enc_k(M)$ . If  $(\zeta, \eta) \in (th)_{(\sigma^l, \rho^r)}$  then  $k \notin \pi_1^l(th)_{(\sigma^l, \rho^r)}$  by Definition 7 for consistency, so  $k \notin \pi_1^l(th')_{(\sigma'^l, \rho'^r)}$ . Else *Max-Dec-Depth* has been used to derive  $e \succ \zeta \leftrightarrow \eta$  when  $\zeta = \sigma'^l(x)$  and  $\eta = \rho'^r(x)$ , so  $\eta = Enc_g(N)$  where  $e \succ k \leftrightarrow g$  and  $e \succ M \leftrightarrow N$ . By Lemma 24  $(k,g) \in e'$  would contradict that e' is un-decreasable. If  $\eta \neq g$  we have by Lemma 33  $e \neq k \leftrightarrow \eta$ . This gives that  $(k, \eta) \notin e'$  so  $k \notin \pi_1^l(th')_{(\sigma'^l, \rho'^r)}$ .

Disjointed consistent evades may be directly combined. Lemma 36: If e' and e are consistent and  $n(e') \cap n(e) = \emptyset$ , then  $e' \cup e$  is consistent.

**Proof:** Take any message pair such that  $(\zeta, \eta) \in \left( (th')_{(\sigma', \rho'')} \cup (th)_{(\sigma', \rho'')} \right)$ . By symmetry we may assume that  $(\zeta, \eta) \in (th')$ 

that  $(\zeta, \eta) \in (th')_{(\sigma'^{l}, \rho'^{r})}$ .

1.  $\zeta \in N \Leftrightarrow \eta \in N$  is clear, since e' is consistent.

2. Take any 
$$(\zeta', \eta') \in \left( (th')_{(\sigma', \rho'')} \cup (th)_{(\sigma', \rho'')} \right)$$
. As  $n(\zeta) \neq \emptyset \neq n(\eta)$  we have that

$$(\zeta',\eta') \in (th')_{(\sigma'^{l},\rho'^{r})}$$
 whenever  $\zeta = \zeta'$  or  $\eta = \eta'$ . As  $e'$  is consistent,  $\zeta = \zeta'$  iff  $\eta = \eta'$ .

3. If 
$$\zeta = Enc_k(\zeta')$$
 and  $\eta = Enc_g(\eta')$  then  $k \notin \pi_1(th')_{\sigma'}$  and  $g \notin \pi_i^r(th')_{(\sigma'})_{(\sigma',\rho')}$  as  $e'$  is

consistent. As  $\{k,g\} \subseteq n(e')$  we have that  $\{k,g\} \cap n(e) \cap fr = \emptyset$  and as a special case of this,

$$k \notin \pi_i^l(th)_{(\sigma^l,\rho^r)}$$
 and  $g \notin \pi_i^r(th)_{(\sigma^l,\rho^r)}$ .

#### **Conclusion And Future works**

The importance of reasoning about knowledge for understanding distributed computations in the field of process algebras has been given some emphasis in recent literature [3, 4, 5, 6, 9, 10, 11, 13]. Furthermore, there have been some formal descriptions of cryptographic protocols [2, 7, 8, 21, 22, 23, 24, 25, 26]. These works have suggested some useful proof techniques. Framed bisimulation is one of the techniques introduced by Abadi and Gordon [2], in which they represent the knowledge of the environment with which the protocol interacts in the form of a frame-theory pair.

Abadi and Gordon defined the *Framed bisimilarity* method as a trend to prove process equivalence based process-environment interactions. Their work represented a restricted attempt that necessitated the existence levels of quantification over infinite domains

Our work follows Abadi and Gordon's framed bisimulation proposal. It introduces a new convenient proof technique called *evade bisimulation*. This technique is proved to detect the limit beyond which the bisimilarity is kept valid and avoids quantification over contexts for output transitions and a finite number of input transitions.

In addition, we have shown that our new bisimilarity method based on spi-<sub>H</sub>-calculus coincides with testing equivalence and we proved that evade bisimulation is a decidable technique for main cryptographic protocols properties, namely: *authenticity* and *confidentiality*. Also, we deem that our technique is simply can be a step toward automation, because of its strong structure in spi-<sub>H</sub>-calculus.

For further work, we believe that it will not be difficult to build evade bisimulation on public-key cryptography. This is something we may look into in the future. We are greatly interested in developing our method toward a symbolic evades bisimulation technique that may enable the automatic verification of cryptographic protocols.

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